



MATH 122

FARMAN

3.1:
DERIVATIVES
OF POLYNOMIALS

CONSTANTS
LINEARITY
POWER RULE

3.2: EXPONENTIAL AND
LOGARITHMIC
FUNCTIONS

MATH 122

Blake Farman ¹

¹University of South Carolina, Columbia, SC USA

Calculus for Business Administration and Social
Sciences



OUTLINE

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1 3.1: DERIVATIVES OF POLYNOMIALS

- Constants
- Linearity
- Power Rule



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DERIVATIVE OF CONSTANTS

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- Let $f(x) = a$ for $a \in \mathbb{R}$ (this means “ a is an element of \mathbb{R} ”, the set of real numbers).



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- Let $f(x) = a$ for $a \in \mathbb{R}$ (this means “ a is an element of \mathbb{R} ”, the set of real numbers).
- The difference quotient for any x_0, x_1 is

$$\frac{f(x_0) - f(x_1)}{x_0 - x_1}$$



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$$\frac{f(x_0) - f(x_1)}{x_0 - x_1} = \frac{a - a}{x_0 - x_1}$$



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$$\frac{f(x_0) - f(x_1)}{x_0 - x_1} = \frac{a - a}{x_0 - x_1} = 0.$$



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- The difference quotient for any x_0, x_1 is

$$\frac{f(x_0) - f(x_1)}{x_0 - x_1} = \frac{a - a}{x_0 - x_1} = 0.$$

- Therefore $f'(x) = 0$.



THE DERIVATIVE IS A LINEAR OPERATOR

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Let f and g be differentiable functions, and let $a \in \mathbb{R}$.



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Let f and g be differentiable functions, and let $a \in \mathbb{R}$.



$$\frac{d}{dx} (f(x) \pm g(x))$$



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$$\frac{d}{dx} (f(x) \pm g(x)) = \frac{d}{dx} f(x) \pm \frac{d}{dx} g(x)$$



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$$\frac{d}{dx} (f(x) \pm g(x)) = \frac{d}{dx} f(x) \pm \frac{d}{dx} g(x)$$



$$\frac{d}{dx} (af(x))$$



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$$\frac{d}{dx} (f(x) \pm g(x)) = \frac{d}{dx} f(x) \pm \frac{d}{dx} g(x)$$



$$\frac{d}{dx} (af(x)) = a \frac{d}{dx} f(x).$$



DERIVATIVE OF A POWER FUNCTIONS

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The derivative of x^n for $n \in \mathbb{R}$ is

$$\frac{d}{dx}(x^n) = nx^{n-1}.$$



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The derivative of x^n for $n \in \mathbb{R}$ is

$$\frac{d}{dx}(x^n) = nx^{n-1}.$$

REMARK 1

The derivative of a linear function is

$$\frac{d}{dx}(mx + b) = m \frac{d}{dx}x + \frac{d}{dx}(b) = m$$



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Consider a degree n polynomial,

$$p(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_2 x^2 + a_1 x + a_0.$$



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$$p(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_2 x^2 + a_1 x + a_0.$$

The derivative is

$$\begin{aligned} p'(x) &= \frac{d}{dx}(a_n x^n + a_{n-1} x^{n-1} + \cdots + a_2 x^2 + a_1 x + a_0) \\ &= a_n \frac{d}{dx}(x^n) + a_{n-1} \frac{d}{dx}(x^{n-1}) + \cdots \\ &\quad + a_2 \frac{d}{dx}(x^2) + a_1 \frac{d}{dx}(x) \end{aligned}$$



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$$p(x) = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_2 x^2 + a_1 x + a_0.$$

The derivative is

$$\begin{aligned} p'(x) &= \frac{d}{dx} (a_n x^n + a_{n-1} x^{n-1} + \cdots + a_2 x^2 + a_1 x + a_0) \\ &= a_n \frac{d}{dx} (x^n) + a_{n-1} \frac{d}{dx} (x^{n-1}) + \cdots \\ &\quad + a_2 \frac{d}{dx} (x^2) + a_1 \frac{d}{dx} (x) \\ &= na_n x^{n-1} + (n-1)a_{n-1} x^{n-2} + \cdots + 2a_2 x + a_1. \end{aligned}$$



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Differentiate the following

1 $A(t) = 3t^5$

2 $r(p) = p^5 + p^3$

3 $f(x) = 5x^2 - 7x^3$

4 $g(t) = \frac{t^2}{4} + 3$



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$$A'(t) =$$



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$$A'(t) = \frac{d}{dt}(3t^5)$$



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$$\begin{aligned} A'(t) &= \frac{d}{dt} (3t^5) \\ &= 3 \left(\frac{d}{dt} (t^5) \right) \end{aligned}$$



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$$\begin{aligned} A'(t) &= \frac{d}{dt} (3t^5) \\ &= 3 \left(\frac{d}{dt} (t^5) \right) \\ &= 3(5t^4) \end{aligned}$$



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$$\begin{aligned} A'(t) &= \frac{d}{dt} (3t^5) \\ &= 3 \left(\frac{d}{dt} (t^5) \right) \\ &= 3(5t^4) \\ &= 15t^4. \end{aligned}$$



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$$r'(p) =$$



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$$r'(p) = \frac{d}{dp} (p^5 + p^3)$$



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$$\begin{aligned} r'(p) &= \frac{d}{dp} (p^5 + p^3) \\ &= \frac{d}{dp} (p^5) + \frac{d}{dp} (p^3) \end{aligned}$$



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$$\begin{aligned} r'(p) &= \frac{d}{dp} (p^5 + p^3) \\ &= \frac{d}{dp} (p^5) + \frac{d}{dp} (p^3) \\ &= 5p^4 + 3p^2. \end{aligned}$$



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$$f'(x) = \frac{d}{dx} (5x^2 - 7x^3)$$



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$$f'(x) = \frac{d}{dx} (5x^2 - 7x^3) = \frac{d}{dx} (5x^2) - \frac{d}{dx} (7x^3)$$



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$$\begin{aligned} f'(x) &= \frac{d}{dx} (5x^2 - 7x^3) = \frac{d}{dx} (5x^2) - \frac{d}{dx} (7x^3) \\ &= 5 \frac{d}{dx} (x^2) - 7 \frac{d}{dx} (x^3) \end{aligned}$$



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$$\begin{aligned} f'(x) &= \frac{d}{dx} (5x^2 - 7x^3) = \frac{d}{dx} (5x^2) - \frac{d}{dx} (7x^3) \\ &= 5 \frac{d}{dx} (x^2) - 7 \frac{d}{dx} (x^3) = 5(2x) - 7(3x^2) \end{aligned}$$



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$$g'(t) = \frac{d}{dt} \left(\frac{t^2}{4} + 3 \right)$$



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4 $g(t) = \frac{t^2}{4} + 3$

$$g'(t) = \frac{d}{dt} \left(\frac{t^2}{4} + 3 \right) = \frac{d}{dt} \left(\frac{t^2}{4} \right) + \frac{d}{dt} (3)$$



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$$\begin{aligned} g'(t) &= \frac{d}{dt} \left(\frac{t^2}{4} + 3 \right) = \frac{d}{dt} \left(\frac{t^2}{4} \right) + \frac{d}{dt} (3) \\ &= \frac{1}{4} \frac{d}{dt} (t^2) + 0 \end{aligned}$$



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$$\begin{aligned}g'(t) &= \frac{d}{dt} \left(\frac{t^2}{4} + 3 \right) = \frac{d}{dt} \left(\frac{t^2}{4} \right) + \frac{d}{dt} (3) \\&= \frac{1}{4} \frac{d}{dt} (t^2) + 0 \\&= \frac{1}{4} (2t)\end{aligned}$$



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$$\begin{aligned}g'(t) &= \frac{d}{dt} \left(\frac{t^2}{4} + 3 \right) = \frac{d}{dt} \left(\frac{t^2}{4} \right) + \frac{d}{dt} (3) \\&= \frac{1}{4} \frac{d}{dt} (t^2) + 0 \\&= \frac{1}{4} (2t) \\&= \frac{t}{2}.\end{aligned}$$



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Find the derivative of

$$f(x) = x^3 - 2x^2 - 5x + 7.$$



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$$f(x) = x^3 - 2x^2 - 5x + 7.$$

$$f'(x) = \frac{d}{dx}(x^3 - 2x^2 - 5x + 7)$$



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Find the derivative of

$$f(x) = x^3 - 2x^2 - 5x + 7.$$

$$\begin{aligned} f'(x) &= \frac{d}{dx}(x^3 - 2x^2 - 5x + 7) \\ &= \frac{d}{dx}(x^3) - \frac{d}{dx}(2x^2) - \frac{d}{dx}(5x) + \frac{d}{dx}(7) \end{aligned}$$



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$$\begin{aligned} f'(x) &= \frac{d}{dx}(x^3 - 2x^2 - 5x + 7) \\ &= \frac{d}{dx}(x^3) - \frac{d}{dx}(2x^2) - \frac{d}{dx}(5x) + \frac{d}{dx}(7) \\ &= \frac{d}{dx}(x^3) - 2\frac{d}{dx}(x^2) - 5\frac{d}{dx}(x) + 0 \end{aligned}$$



EXAMPLE

MATH 122

FARMAN

3.1:
DERIVATIVES
OF POLYNOMIALS

CONSTANTS

LINEARITY

POWER RULE

3.2: EXPO-
NENTIAL AND
LOGARITH-
MIC
FUNCTIONS

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EXPONENTIALS

MATH 122

FARMAN

3.1:
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FUNCTIONS

The derivative of e^x is

$$\frac{d}{dx}(e^x) = e^x.$$



LOGARITHMS

MATH 122

FARMAN

3.1:
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LINEARITY
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- The derivative of the natural logarithm is

$$\frac{d}{dx}(\ln(x)) = \frac{1}{x}.$$



LOGARITHMS

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LOGARITHMS

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LOGARITHMS

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