

### Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS 1.2: LINEAR FUNCTIONS

# Матн 122

### Blake Farman<sup>1</sup>

<sup>1</sup>University of South Carolina, Columbia, SC USA

# Calculus for Business Administration and Social Sciences

▲□▶ ▲□▶ ▲臣▶ ▲臣▶ ―臣 – のへで



# OUTLINE

МАТН 122

FARMAN

1.1: FUNCTIONS Graphs

1.2: LINEAR Functions

# 1.1: FUNCTIONSGraphs

- イロト イ理ト イヨト イヨト ヨー のへぐ



### **OUTLINE**

**MATH 122** 

### **1** 1.1: FUNCTIONS • Graphs

**2** 1.2: LINEAR FUNCTIONS

◆ロト ◆課 ト ◆注 ト ◆注 ト ・注 ・ のへで



#### МАТН 122

FARMAN

#### 1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS

### **DEFINITION 1**

• A *function* is a rule that takes certain values as inputs and assigns to each input **exactly one** output.

▲ロト ▲周 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()



#### МАТН 122

FARMAN

#### 1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS

### **DEFINITION** 1

- A *function* is a rule that takes certain values as inputs and assigns to each input **exactly one** output.
- The set of all possible inputs is called the *domain* of the function.

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0



#### МАТН 122

FARMAN

#### 1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS

### **DEFINITION** 1

- A *function* is a rule that takes certain values as inputs and assigns to each input **exactly one** output.
- The set of all possible inputs is called the *domain* of the function.
- The set of all possible outputs is called the *range* of the function.

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0



**DEFINITION 1** 

#### МАТН 122

FARMAN

#### 1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS

- A *function* is a rule that takes certain values as inputs and assigns to each input **exactly one** output.
  - The set of all possible inputs is called the *domain* of the function.
  - The set of all possible outputs is called the *range* of the function.

Notation: A function named f that takes as input the *independent variable*, x, and outputs the *dependent variable*, y, is written as

$$y=f(x).$$

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0



#### Матн 122

FARMAN

#### 1.1: Functions

GRAPHS

**1.2:** LINEAR FUNCTIONS

Given any two sets we can define a function.





МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .



МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS

### Define

Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .



МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .

Define

• f(1) = 6

• f(2) = 5



МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .

Define

• f(1) = 6

• f(3) = 8



МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .

Define

• f(1) = 6

• f(3) = 8



МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .

Define

• f(1) = 6

• f(3) = 8





МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .

Define

• f(1) = 6

• f(3) = 8





МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .

Define

• f(1) = 6

• f(3) = 8





МАТН 122

FARMAN

1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS Given any two sets we can define a function. Say we have the sets

$$D = \{1, 2, 3, 4\}$$
 and  $R = \{5, 6, 7, 8\}$ .

Define

• f(1) = 6

• f(3) = 8





### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS The function  $f(x) = x^2$  is a function.



#### МАТН 122

FARMAN

#### 1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS The function  $f(x) = x^2$  is a function.

• The domain of f is the set of all real numbers,  $\mathbb{R}$ .



#### МАТН 122

FARMAN

#### 1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS The function  $f(x) = x^2$  is a function.

- The domain of f is the set of all real numbers,  $\mathbb{R}$ .
- The range of *f* is the set of all non-negative real numbers,

$$\{x\in\mathbb{R}\mid 0\leq x\}\,.$$

<ロト < 同ト < 三ト < 三ト < 三ト < ○へ</p>



### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS The following depicts a non-function.



### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS

### The following depicts a non-function.



◆□ > ◆□ > ◆臣 > ◆臣 > ─臣 = のへで



### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS

### The following depicts a non-function.





### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS

### The following depicts a non-function.





### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS

### The following depicts a non-function.





### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS

### The following depicts a non-function.



◆□ > ◆□ > ◆臣 > ◆臣 > ─臣 = のへで



### МАТН 122

FARMAN

#### 1.1: FUNCTIONS

GRAPHS

1.2: LINEAR FUNCTIONS

### The following depicts a non-function.





#### **MATH 122**

FARMAN

#### 1.1: Functions

GRAPHS

1.2: LINEAR FUNCTIONS

### The following depicts a non-function.



The value f(1) is not well-defined because it requires a choice: it could be either 6 or 8.



# CARTESIAN PLANE

Матн 122

FARMAN

1.1: Functions graphs

1.2: LINEAR FUNCTIONS Recall that the *Cartesian plane* is the set of all pairs

$$\mathbb{R}^2 = \{(x, y) \mid x \in \mathbb{R}, y \in \mathbb{R}\}.$$

<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >



## CARTESIAN PLANE

Матн 122

FARMAN

1.1: Functions graphs

1.2: LINEAR FUNCTIONS Recall that the *Cartesian plane* is the set of all pairs  $\mathbb{R}^2 = \{(x, y) \mid x \in \mathbb{R}, y \in \mathbb{R}\}.$ 

It can be depicted as





### **GRAPH OF A FUNCTION**

### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS 1.2: LINEAF

### **DEFINITION 2**

The graph of a real-valued function, f, with domain  $D \subseteq \mathbb{R}$  is the set of pairs

$$\{(x, f(x)) \mid x \in D\} \subseteq \mathbb{R}^2.$$

▲ロト ▲周 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()

It can be drawn on the Cartesian plane.



### МАТН 122

FARMAN

1.1: Functions graphs 1.2: Linear

### The function f(x) = x has



### МАТН 122

FARMAN

1.1: Functions graphs 1.2: Linear The function f(x) = x has

• Domain all real numbers,  $\mathbb{R}$ ,



#### МАТН 122

FARMAN

1.1: Functions graphs

1.2: LINEAR FUNCTIONS The function f(x) = x has

- Domain all real numbers,  $\mathbb{R}$ ,
- Range all real numbers,  $\mathbb{R}$ ,

▲□▶ ▲□▶ ▲臣▶ ▲臣▶ 三臣 - のへで



#### МАТН 122

FARMAN

1.1: Functions graphs 1.2: Line at

1.2: LINEAR Functions

### The function f(x) = x has

- Domain all real numbers,  $\mathbb{R}$ ,
- Range all real numbers,  $\mathbb{R}$ ,

▲ロト ▲周 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()

• Graph  $\{(x, x) \mid x \in \mathbb{R}\},\$ 



#### МАТН 122

FARMAN

1.1: Functions graphs 1.2: Linear The function f(x) = x has

- Domain all real numbers,  $\mathbb{R}$ ,
- Range all real numbers,  $\mathbb{R}$ ,
- Graph  $\{(x, x) \mid x \in \mathbb{R}\}$ ,



▲ロト ▲周 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()


#### МАТН 122

FARMAN

1.1: Functions graphs 1.2: Linear Functions

### **DEFINITION 3**

Let f be a function and let [a, b] be an interval contained in the domain of f. We say f is

▲□▶▲□▶▲□▶▲□▶ □ のQで



### **MATH 122**

FARMAN

### 1.1: Functions graphs 1.2: Linear Functions

### DEFINITION 3

Let f be a function and let [a, b] be an interval contained in the domain of f. We say f is

▲□▶ ▲□▶ ▲三▶ ▲三▶ - 三 - つへで

 increasing on [a,b] if f(x<sub>1</sub>) < f(x<sub>2</sub>) whenever a ≤ x<sub>1</sub> < x<sub>2</sub> ≤ b,



### MATH 122

FARMAN

### 1.1: Functions graphs 1.2: Linear Functions

### DEFINITION 3

Let f be a function and let [a, b] be an interval contained in the domain of f. We say f is

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0

- increasing on [a,b] if  $f(x_1) < f(x_2)$  whenever  $a \le x_1 < x_2 \le b$ ,
- decreasing on [a,b] if  $f(x_2) < f(x_1)$  whenever  $a \le x_1 < x_2 \le b$ .



### MATH 122

FARMAN

### 1.1: Functions graphs 1.2: Linear Functions

### DEFINITION 3

Let f be a function and let [a, b] be an interval contained in the domain of f. We say f is

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0

- increasing on [a,b] if  $f(x_1) < f(x_2)$  whenever  $a \le x_1 < x_2 \le b$ ,
- decreasing on [a,b] if  $f(x_2) < f(x_1)$  whenever  $a \le x_1 < x_2 \le b$ .

We say that f is increasing/decreasing if it is increasing/decreasing on its entire domain.



Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS 1.2: LINEAL



◆□▶ ◆□▶ ◆ □▶ ◆ □ ▶ ● □ ● ● ● ●



**MATH 122** 

## EXAMPLE

1.1: Functions Graphs 1.2: Linear



- Increasing on:
- Decreasing on:



**MATH 122** 

## EXAMPLE

1.1: Functions graphs 1.2: Linear



<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >

- Increasing on:  $(0,\infty)$
- Decreasing on:



**MATH 122** 

## EXAMPLE

1.1: Functions graphs 1.2: Linear



▲□▶ ▲□▶ ▲□▶ ▲□▶ = 三 のへで

- Increasing on:  $(0,\infty)$
- Decreasing on:  $(-\infty, 0)$





◆□▶ ◆□▶ ◆ □▶ ◆ □ ▶ ● □ ● ● ● ●







# INTERCEPTS

M	ATH	12	2

FARMAN

1.1: Functions graphs

1.2: LINEAR FUNCTIONS

### **DEFINITION 4**

Let *f* be a function of a real variable, *x*.



## INTERCEPTS

### **MATH 122**

FARMAN

1.1: Functions graphs

1.2: LINEAR FUNCTIONS

### **DEFINITION 4**

Let *f* be a function of a real variable, *x*.

• The *x*-intercepts are the points (x, 0) on the graph.

▲□▶ ▲□▶ ▲□▶ ▲□▶ = 三 のへで



## INTERCEPTS

### **MATH 122**

FARMAN

1.1: Functions graphs

1.2: LINEAR FUNCTIONS

### **DEFINITION 4**

Let f be a function of a real variable, x.

- The *x*-intercepts are the points (x, 0) on the graph.
- The *y*-intercept is the point (0, f(0)) on the graph.

◆□▶ ◆□▶ ◆□▶ ◆□▶ → □ ・ つくぐ



МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS Let f(x) = x - 1.





Матн 122

FARMAN

1.1: Functions Graphs 1.2: Linear Let f(x) = x - 1. The *y*-intercept is

$$(0, f(0)) = (0, 0 - 1) = (0, -1).$$



Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS Let f(x) = x - 1. The *y*-intercept is

$$(0, f(0)) = (0, 0 - 1) = (0, -1).$$

The x – *intercept* is (1,0):

$$f(1) = 1 - 1 = 0.$$

<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >



Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS 1.2: LINEAR Let f(x) = x - 1. The *y*-intercept is

$$(0, f(0)) = (0, 0 - 1) = (0, -1).$$

The x – *intercept* is (1,0):







#### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### DEFINITION 5

A function, *f*, is *linear* if there exist real numbers *m* and *b* such that

$$f(x)=mx+b.$$



### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### DEFINITION 5

A function, *f*, is *linear* if there exist real numbers *m* and *b* such that

$$f(x)=mx+b.$$

▲ロト ▲周 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()

• Linear functions have domain and range  $\mathbb{R},$ 



### МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### DEFINITION 5

A function, *f*, is *linear* if there exist real numbers *m* and *b* such that

$$f(x)=mx+b.$$

▲□▶▲□▶▲□▶▲□▶ □ のQで

- Linear functions have domain and range  $\mathbb{R},$
- The number *m* is called the *slope* of the *f*,



### MATH 122

FARMAN

1.1: FUNCTIONS GRAPHS

FUNCTIONS

**DEFINITION 5** 

A function, *f*, is *linear* if there exist real numbers *m* and *b* such that

$$f(x)=mx+b.$$

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0

- Linear functions have domain and range  $\mathbb{R},$
- The number *m* is called the *slope* of the *f*,
- The number b is the y-intercept,



### МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS

FUNCTIONS

### **DEFINITION 5**

A function, *f*, is *linear* if there exist real numbers *m* and *b* such that

$$f(x)=mx+b.$$

- Linear functions have domain and range  $\mathbb{R}$ ,
- The number *m* is called the *slope* of the *f*,
- The number b is the y-intercept,
- This form is usually called the *Slope-Intercept Form* of a line.



#### Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS The graph of f(x) = mx + b is always a line.

◆ロト ◆課 ト ◆注 ト ◆注 ト ・注 ・ のへで



#### Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS The graph of f(x) = mx + b is always a line. They come in three flavors:



#### МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS The graph of f(x) = mx + b is always a line. They come in three flavors:

• Increasing (0 < *m*):



#### МАТН 122

FARMAN

1.1: FUNCTIONS Graphs

1.2: LINEAR FUNCTIONS The graph of f(x) = mx + b is always a line. They come in three flavors:

◆□▶ ◆□▶ ◆□▶ ◆□▶ → □ ・ つくぐ

• Increasing (0 < *m*):

• Decreasing (*m* < 0):



#### МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS The graph of f(x) = mx + b is always a line. They come in three flavors:

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0

• Increasing (0 < *m*):

• Decreasing (*m* < 0):

• Horizontal (m = 0):



### Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### **DEFINITION 6**

Given:



### Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### DEFINITION 6

### Given:

• a point,  $(x_0, y_0)$ ,





### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### DEFINITION 6

### Given:

• a point,  $(x_0, y_0)$ ,

◆ロト ◆課 ト ◆注 ト ◆注 ト ・注 ・ のへで

• a slope, *m*,



### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### DEFINITION 6

Given:

- a point,  $(x_0, y_0)$ ,
- a slope, *m*,

the equation of the line through  $(x_0, y_0)$  with slope *m* is

$$y-y_0=m(x-x_0).$$



# Two Points Determine a Line

### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS 1.2: LINEAR

FUNCTIONS

Given two points,  $(x_0, y_0)$  and  $(x_1, y_1)$ , the slope of the line passing through them is

$$m = \frac{y_0 - y_1}{x_0 - x_1} = \frac{y_1 - y_0}{x_1 - x_0}.$$



# Two Points Determine a Line

### МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS 1.2: LINEAR

FUNCTIONS

Given two points,  $(x_0, y_0)$  and  $(x_1, y_1)$ , the slope of the line passing through them is

$$m = \frac{y_0 - y_1}{x_0 - x_1} = \frac{y_1 - y_0}{x_1 - x_0}$$

The line passing through these two points is

$$y - y_0 = m(x - x_0)$$
 or  $y - y_1 = m(x - x_1)$ .



# Two Points Determine a Line

### MATH 122

FARMAN

1.1: FUNCTIONS GRAPHS 1.2: LINEAR

FUNCTIONS

Given two points,  $(x_0, y_0)$  and  $(x_1, y_1)$ , the slope of the line passing through them is

$$m = \frac{y_0 - y_1}{x_0 - x_1} = \frac{y_1 - y_0}{x_1 - x_0}$$

The line passing through these two points is

$$y - y_0 = m(x - x_0)$$
 or  $y - y_1 = m(x - x_1)$ .

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0

To see these are the same line, put them both into Slope-Intercept Form.



# Two Points Determine a Line (Cont.)

МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

$$y = mx - \frac{y_0 - y_1}{x_0 - x_1}x_0 + y_0$$

$$y = mx - \frac{y_0 - y_1}{x_0 - x_1}x_1 + y_1$$

◆□▶ ◆□▶ ◆ □▶ ◆ □ ● ● ● ●



# Two Points Determine a Line (Cont.)

Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

$$y = mx - \frac{y_0 - y_1}{x_0 - x_1} x_0 + y_0$$
  
=  $mx + \frac{(y_1 - y_0)x_0 + (x_0 - x_1)y_0}{x_0 - x_1}$ 

$$y = mx - \frac{y_0 - y_1}{x_0 - x_1} x_1 + y_1$$
  
=  $mx + \frac{(y_1 - y_0)x_1 + (x_0 - x_1)y_1}{x_0 - x_1}$ 

▲ロト ▲御 ト ▲臣 ト ▲臣 ト → 臣 → の々ぐ


### Two Points Determine a Line (Cont.)

Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

$$y = mx - \frac{y_0 - y_1}{x_0 - x_1} x_0 + y_0$$
  
=  $mx + \frac{(y_1 - y_0)x_0 + (x_0 - x_1)y_0}{x_0 - x_1}$   
=  $mx - \frac{x_0y_1 - x_1y_0}{x_0 - x_1}$ 

$$y = mx - \frac{y_0 - y_1}{x_0 - x_1} x_1 + y_1$$
  
=  $mx + \frac{(y_1 - y_0)x_1 + (x_0 - x_1)y_1}{x_0 - x_1}$   
=  $mx + \frac{x_0y_1 - x_1y_0}{x_0 - y_0}$ 

▲□▶▲圖▶▲厘▶▲厘▶ 厘 のへで



#### Матн 122

FARMAN

1.1: FUNCTIONS

1.2: LINEAR FUNCTIONS

### **DEFINITION 7**

Let f be a function.



#### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### **DEFINITION 7**

Let *f* be a function. Given  $x_0$ ,  $x_1$  in the domain of *f* 

▲□▶ ▲□▶ ▲□▶ ▲□▶ = 三 のへで



#### Матн 122

FARMAN

1.1: FUNCTION GRAPHS

1.2: LINEAR FUNCTIONS

### **DEFINITION 7**

Let *f* be a function. Given  $x_0$ ,  $x_1$  in the domain of *f*, the *difference quotient* is

$$\frac{f(x_1) - f(x_0)}{x_1 - x_0} = \frac{f(x_0) - f(x_1)}{x_0 - x_1}$$

▲ロト ▲周 ト ▲ ヨ ト ▲ ヨ ト ・ ヨ ・ の Q ()



#### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR Functions

### DEFINITION 7

Let *f* be a function. Given  $x_0$ ,  $x_1$  in the domain of *f*, the *difference quotient* is

$$\frac{f(x_1) - f(x_0)}{x_1 - x_0} = \frac{f(x_0) - f(x_1)}{x_0 - x_1}$$

▲□▶ ▲□▶ ▲目▶ ▲目▶ 三目 - のへぐ

This is just the slope of the line through  $(x_0, f(x_0))$  and  $(x_1, f(x_1))$ .



#### **MATH 122**

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

### DEFINITION 7

Let *f* be a function. Given  $x_0$ ,  $x_1$  in the domain of *f*, the *difference quotient* is

$$\frac{f(x_1) - f(x_0)}{x_1 - x_0} = \frac{f(x_0) - f(x_1)}{x_0 - x_1}$$

<ロト < 同ト < 目ト < 目 > < 日 > < 回 > < 0 < 0

This is just the slope of the line through  $(x_0, f(x_0))$  and  $(x_1, f(x_1))$ . This line is usually called the *Secant Line*.



#### МАТН 122

FARMAN







◆ロト ◆課 ト ◆注 ト ◆注 ト ・注 ・ のへで

#### **MATH 122**

FARMAN

1.1: Functions Graphs

1.2: LINEAR FUNCTIONS Let f(x) = mx + b. Given  $x_0$  and  $x_1$ :



МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

Let 
$$f(x) = mx + b$$
. Given  $x_0$  and  $x_1$ :  

$$\frac{f(x_1) - f(x_0)}{x_1 - x_0} = \frac{mx_1 + b - (mx_0 + b)}{x_1 - x_0}$$



МАТН 122

FARMAN

Let

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

$$f(x) = mx + b. \text{ Given } x_0 \text{ and } x_1:$$

$$\frac{f(x_1) - f(x_0)}{x_1 - x_0} = \frac{mx_1 + b - (mx_0 + b)}{x_1 - x_0}$$

$$= \frac{mx_1 - mx_0 + b - b}{x_1 - x_0}$$

◆ロト ◆課 ト ◆注 ト ◆注 ト ・注 ・ のへで



МАТН 122

FARMAN

Let f

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

$$(x) = mx + b. \text{ Given } x_0 \text{ and } x_1:$$

$$\frac{f(x_1) - f(x_0)}{x_1 - x_0} = \frac{mx_1 + b - (mx_0 + b)}{x_1 - x_0}$$

$$= \frac{mx_1 - mx_0 + b - b}{x_1 - x_0}$$

$$= \frac{m(x_1 - x_0)}{x_1 - x_0}$$

◆ロト ◆課 ト ◆注 ト ◆注 ト ・注 ・ のへで



МАТН 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

Let $f(x) = mx + b$ . Given $x_0$ and $x_1$ :		
$\frac{f(x_1) - f(x_0)}{x_1 - x_2}$	=	$\frac{mx_1+b-(mx_0+b)}{x_1-x_2}$
A1 A0	=	$\frac{mx_1 - mx_0 + b - b}{x_1 - x_0}$
	=	$\frac{m(x_1 - x_0)}{x_1 - x_0}$
	=	m

◆ロト ◆課 ト ◆注 ト ◆注 ト ・注 ・ のへで



МАТН 122

FARMAN

1.1: FUNCTIONS Graphs

1.2: LINEAR FUNCTIONS

Let $f(x) = mx + b$ . Given $x_0$ and $x_1$ :			
$\underline{f(x_1)-f(x_0)}$	=	$\underline{mx_1 + b - (mx_0 + b)}$	
$x_1 - x_0$		$x_1 - x_0$	
	_	$\underline{mx_1 - mx_0 + b - b}$	
		$x_1 - x_0$	
	=	$m(x_1 - x_0)$	
		$x_1 - x_0$	
	=	т	

Hence for a linear function, the difference quotient is just the slope.

▲□▶ ▲□▶ ▲□▶ ▲□▶ = 三 のへで



<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >

МАТН 122

FARMAN

Let 
$$f(x) = x^2$$
. For  $x_0 = -1$ ,  $x_1 = 2$ :

1.1: FUNCTIONS GRAPHS



**MATH 122** 

FARMAN

1.1: FUNCTIONS GRAPHS

Let  $f(x) = x^2$ . For  $x_0 = -1$ ,  $x_1 = 2$ :

$$\frac{f(-1)-f(2)}{-1-2}$$



<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >

Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

Let 
$$f(x) = x^2$$
. For  $x_0 = -1$ ,  $x_1 = 2$ :

$$\frac{f(-1)-f(2)}{-1-2}=\frac{(-1)^2-2^2}{-3}$$



Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

Let 
$$f(x) = x^2$$
. For  $x_0 = -1$ ,  $x_1 = 2$ :

$$\frac{f(-1) - f(2)}{-1 - 2} = \frac{(-1)^2 - 2^2}{-3} = \frac{1 - 4}{-3}$$

<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >



0

Матн 122

FARMAN

1.1: FUNCTIONS GRAPHS

1.2: LINEAR FUNCTIONS

Let 
$$f(x) = x^2$$
. For  $x_0 = -1$ ,  $x_1 = 2$ :  
$$\frac{f(-1) - f(2)}{-1 - 2} = \frac{(-1)^2 - 2^2}{-3} = \frac{1 - 4}{-3} = \frac{-3}{-3} = 1.$$

▲□▶ ▲□▶ ▲□▶ ▲□▶ = 三 のへで



**MATH 122** 

FARMAN

1.1: Functions Graphs

1.2: LINEAR FUNCTIONS

Let 
$$f(x) = x^2$$
. For  $x_0 = -1$ ,  $x_1 = 2$ :

$$\frac{f(-1)-f(2)}{-1-2} = \frac{(-1)^2 - 2^2}{-3} = \frac{1-4}{-3} = \frac{-3}{-3} = 1.$$

This is the slope of the secant line:



▲□▶ ▲□▶ ▲□▶ ▲□▶ = 三 のへで



▲□▶ ▲□▶ ▲臣▶ ▲臣▶ ―臣 – のへぐ

МАТН 122

FARMAN

For 
$$x_0 = 0$$
,  $x_1 = 2$ :

1.1: FUNCTIONS GRAPHS



<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >

МАТН 122

FARMAN

For 
$$x_0 = 0$$
,  $x_1 = 2$ :

1.1: FUNCTIONS Graphs

$$\frac{f(0)-f(2)}{0-2}$$



МАТН 122

FARMAN

For 
$$x_0 = 0$$
,  $x_1 = 2$ :

$$\frac{f(0)-f(2)}{0-2}=\frac{0-4}{-2}$$

<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >



МАТН 122

FARMAN

For 
$$x_0 = 0$$
,  $x_1 = 2$ :

$$\frac{f(0)-f(2)}{0-2}=\frac{0-4}{-2}=\frac{4}{2}=2.$$

<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >



Матн 122

FARMAN

For 
$$x_0 = 0$$
,  $x_1 = 2$ :

$$\frac{f(0)-f(2)}{0-2}=\frac{0-4}{-2}=\frac{4}{2}=2.$$

1.2: LINEAR FUNCTIONS

This is the slope of the secant line:



▲□▶ ▲□▶ ▲臣▶ ▲臣▶ ―臣 – のへぐ